

Basic Electrical Engineering

ECS 203

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7. Sinusoids and Phasors



Office Hours:

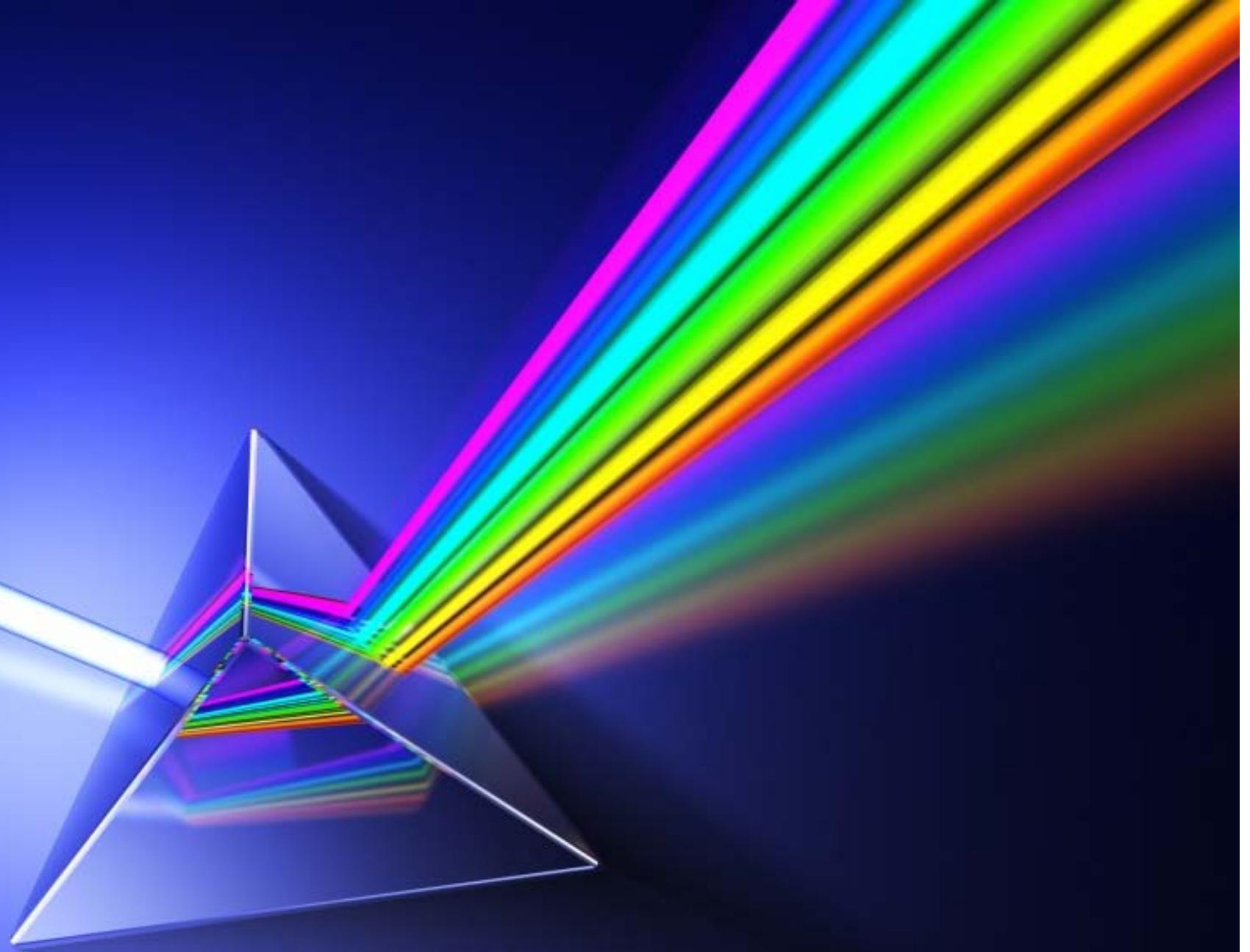
BKD, 4th floor of Sirindhralai building

Monday 14:00-16:00

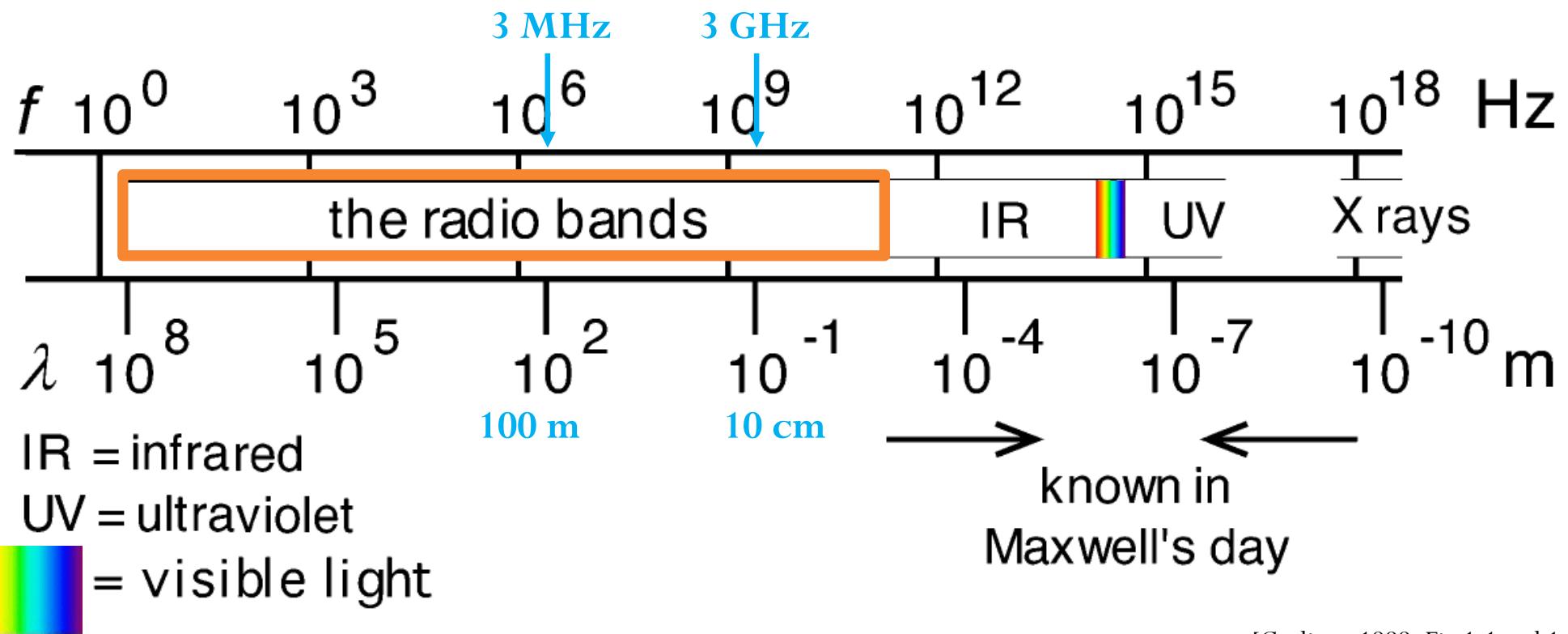
Thursday 10:30-11:30

Friday 12:00-13:00





Electromagnetic Spectrum



[Gosling, 1999, Fig 1.1 and 1.2]

f	Hz	kHz			MHz			GHz		
	300	3	30	300	3	30	300	3	30	
ELF	SLF	VLF	LF	MF	HF	VHF	UHF	SHF	EHF	
1	100	10	1	100	10	1	100	10		
Mega metre	kilometres			metres			millimetres			

$$c = f\lambda$$

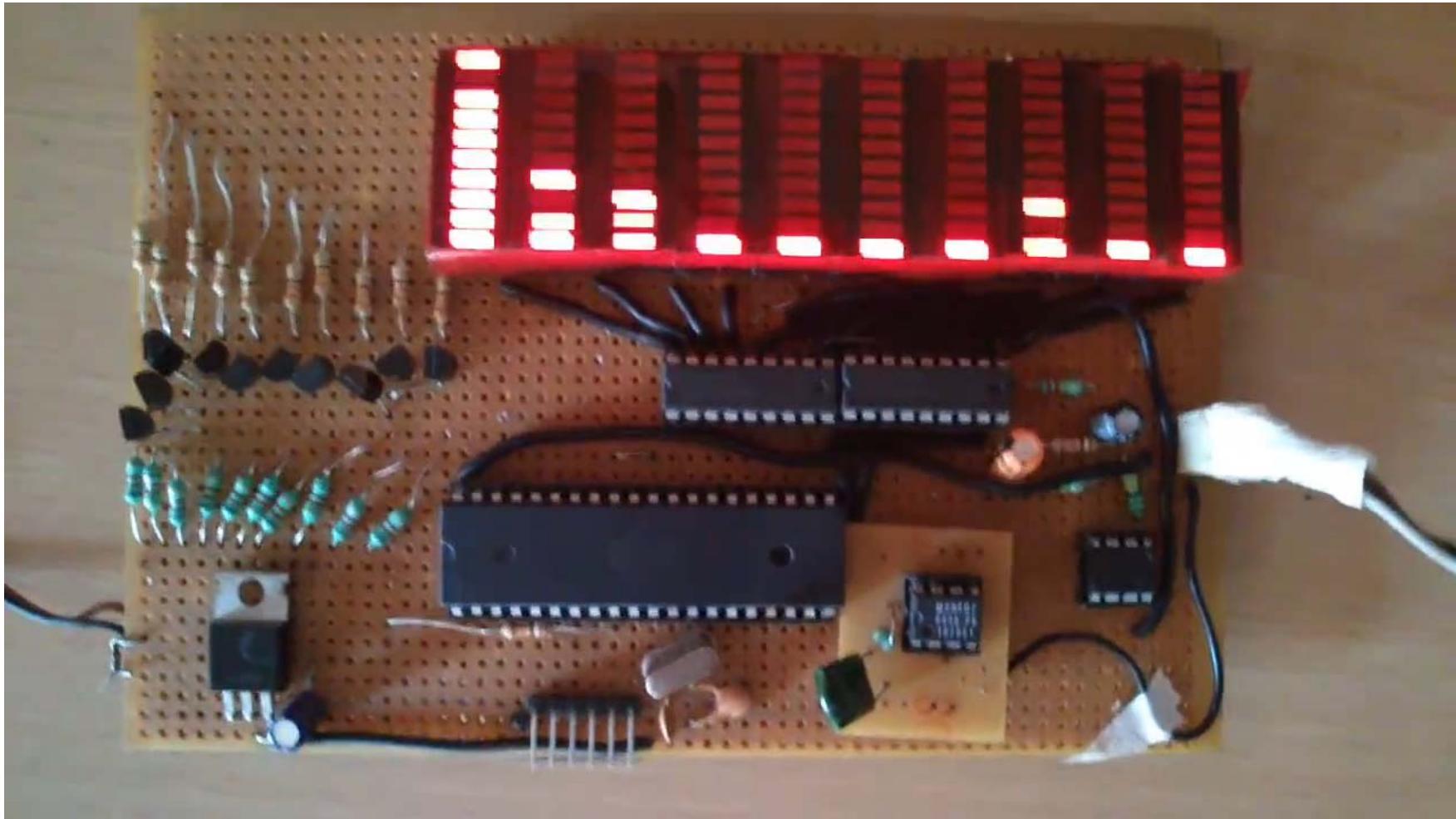
3 \times 10⁸ m/s

Wavelength

Frequency

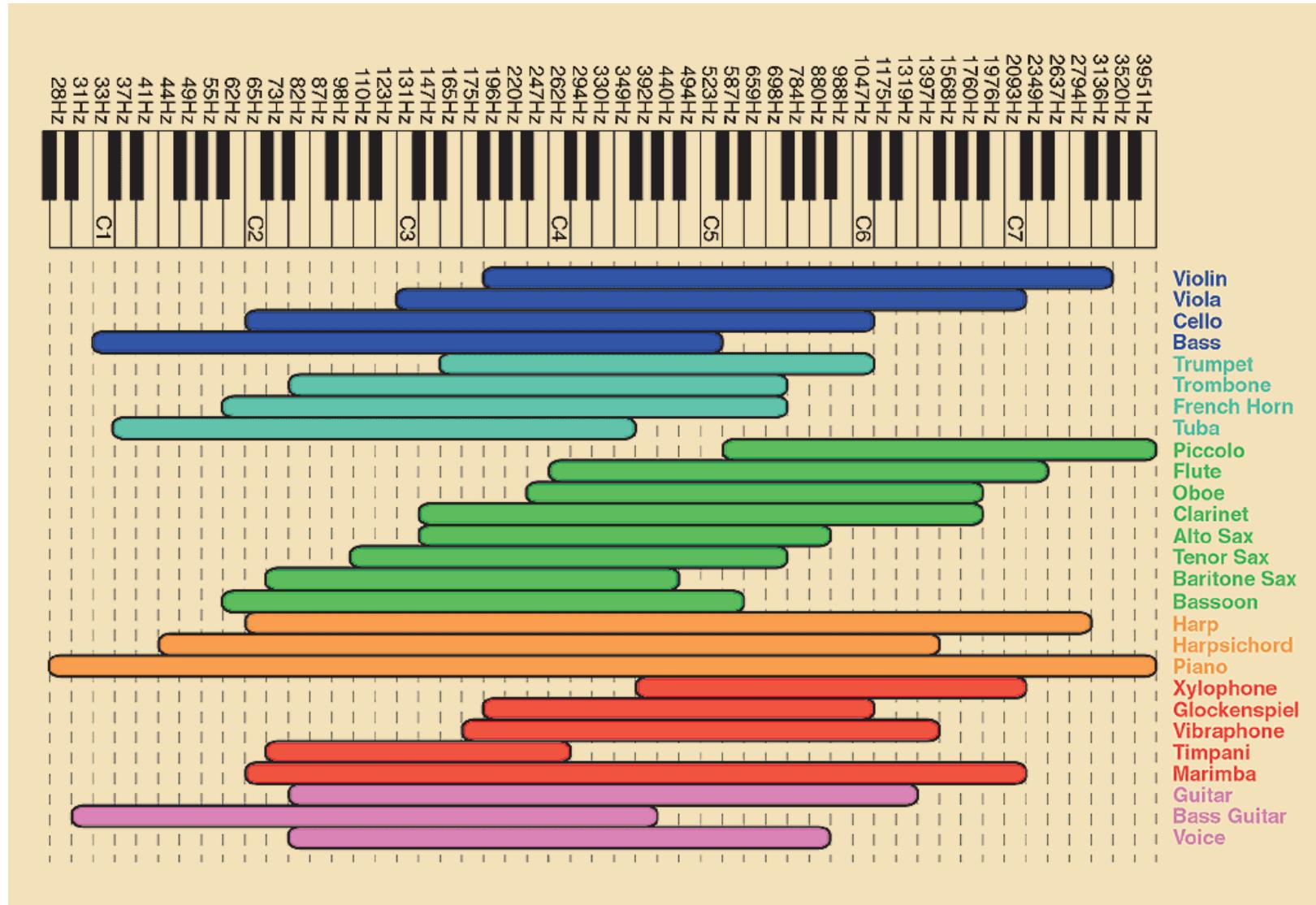
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LED Audio Spectrum Analyzer



The (Fundamental) Frequencies of Musical Instruments

Note frequency



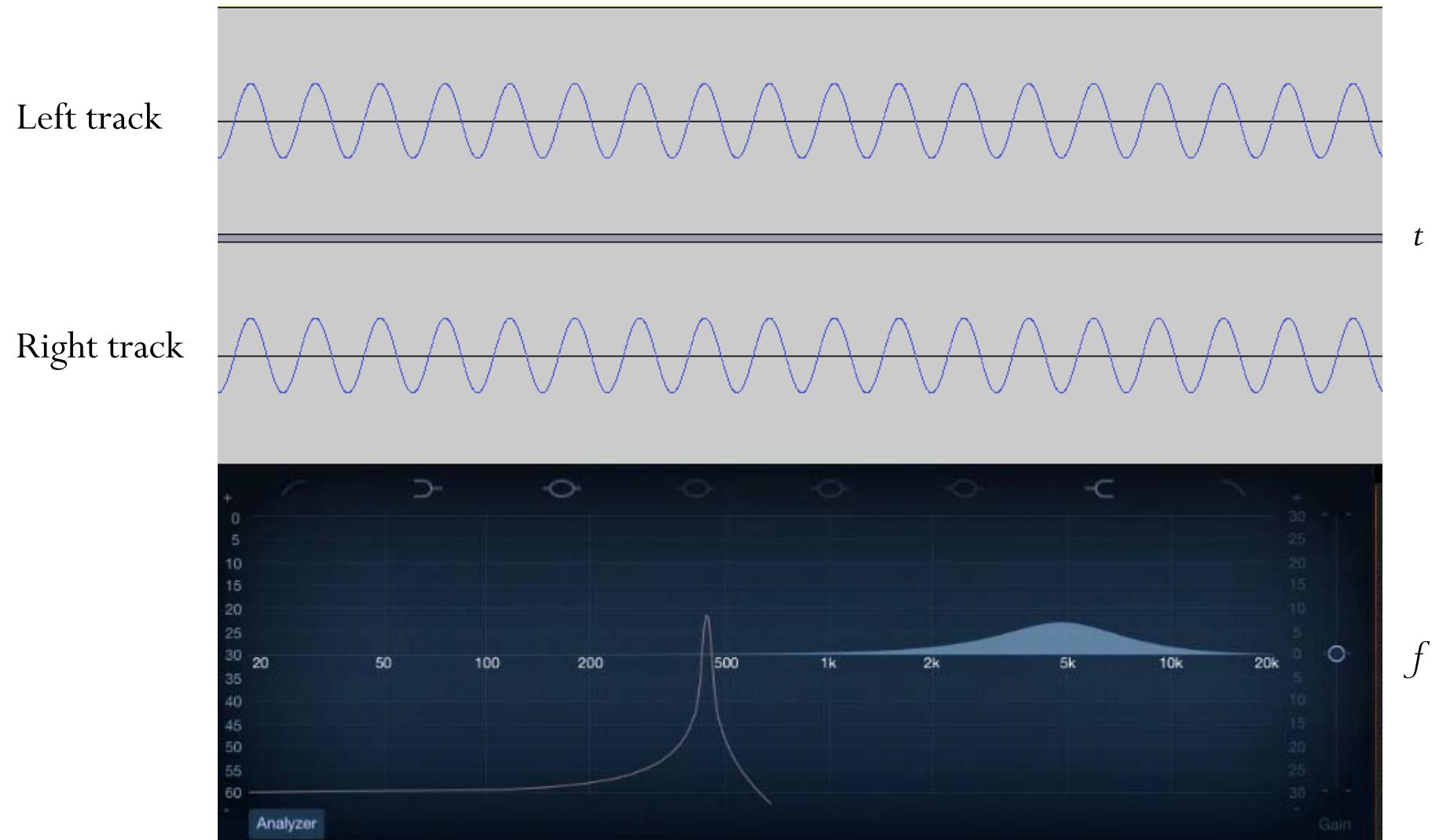
A440 on Different Instruments

“Same”
timbre of a
tuning fork
(“pure”
tone)

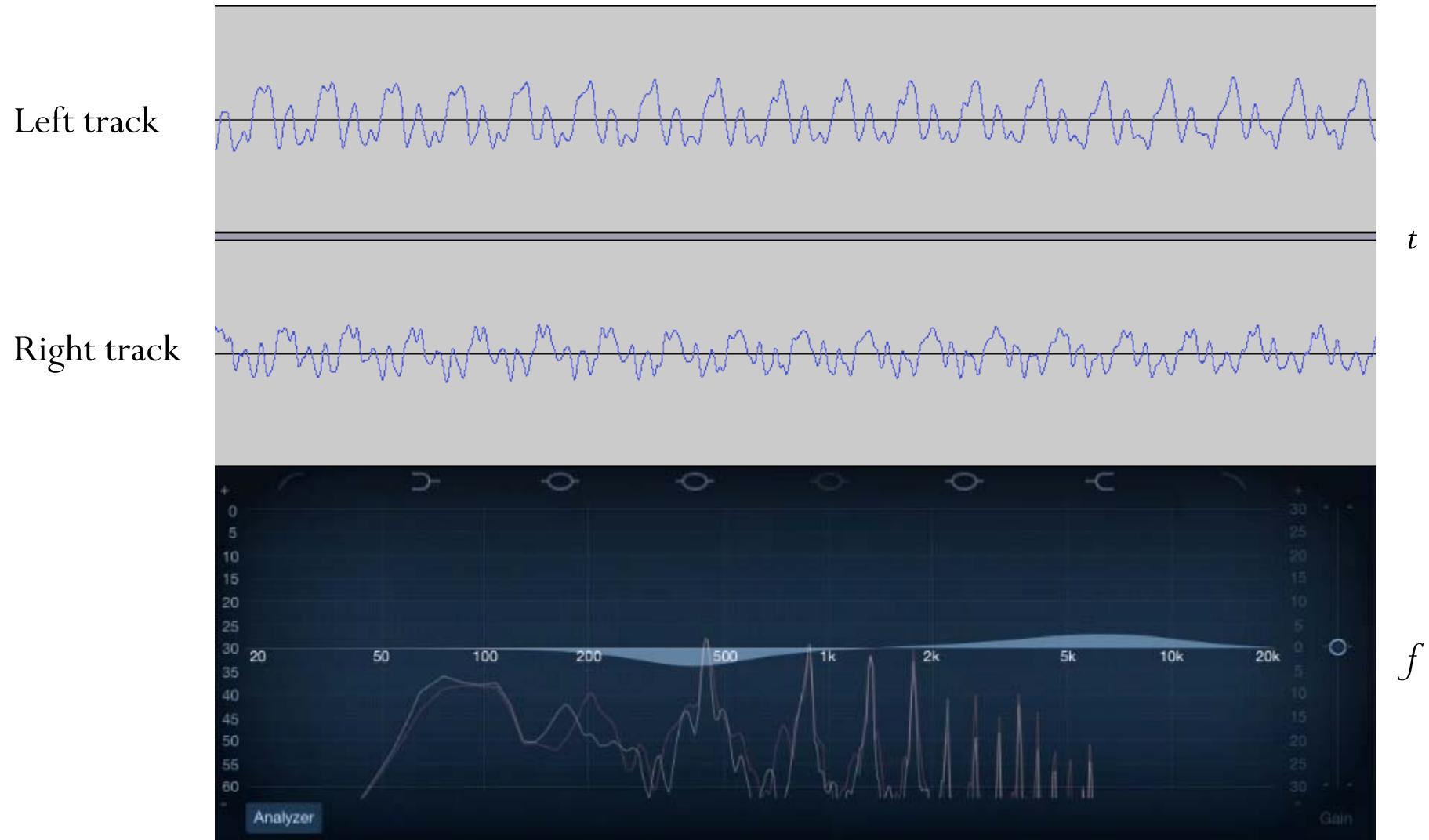


[GarageBand]

A440 on a Cathedral Organ



A440 on a Grand Piano



Tone Dialing



- Most modern telephones use a dialing system known as **Touch-Tone**.
 - **Dual-tone multifrequency (DTMF) system.**
- Use **pairs of audio** (voice-frequency) **tones** to create signals representing the numbers to be dialed.
- First developed in the **Bell System** in the United States, and became known under the trademark **Touch-Tone** for use in push-button telephones starting in 1963.
 - Replace the use of **rotary dial**.
- Standardized by ITU-T Recommendation Q.23.
 - Also known in the UK as MF4.



Tests in regular service last winter at Carnegie and Greensburg, Pa., suburbs of Pittsburgh, have shown it's easier and more than twice as fast to press buttons for a phone call than it is to twirl a dial. As each "touch-tone" button is pushed, it sounds a pleasing musical tone.

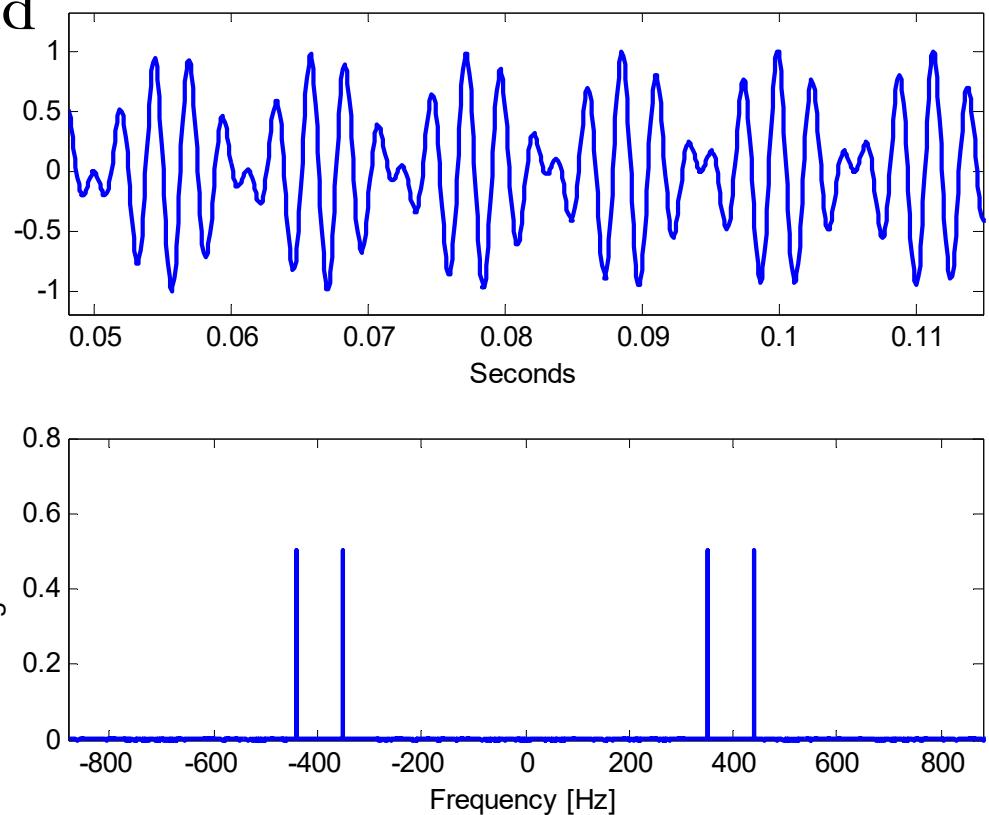
Bell is introducing the phone area by area, will have it in general use within the next 10 years.

[Apr, 1964]

Dial Tone

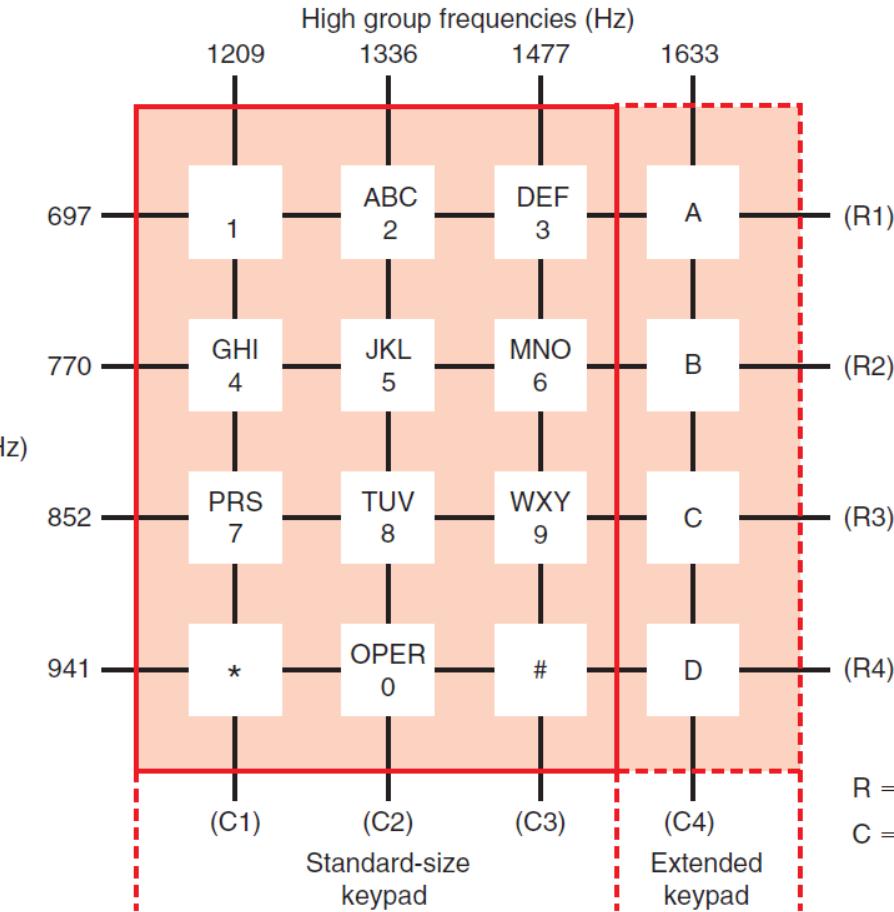


- North American and UK: A continuous mix of 350 Hz and 440 Hz
 - These two frequencies correspond to the standard concert pitch of A440, and approximately an “F”.
 - $\text{@ } -12\text{dBm}$
- Most of Europe: constant single tone (425 Hz)



Encoding

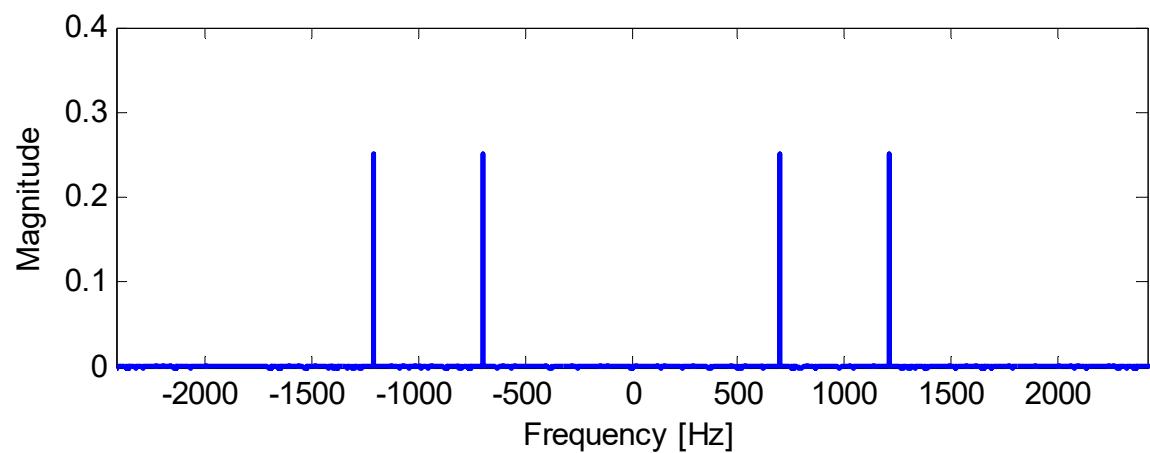
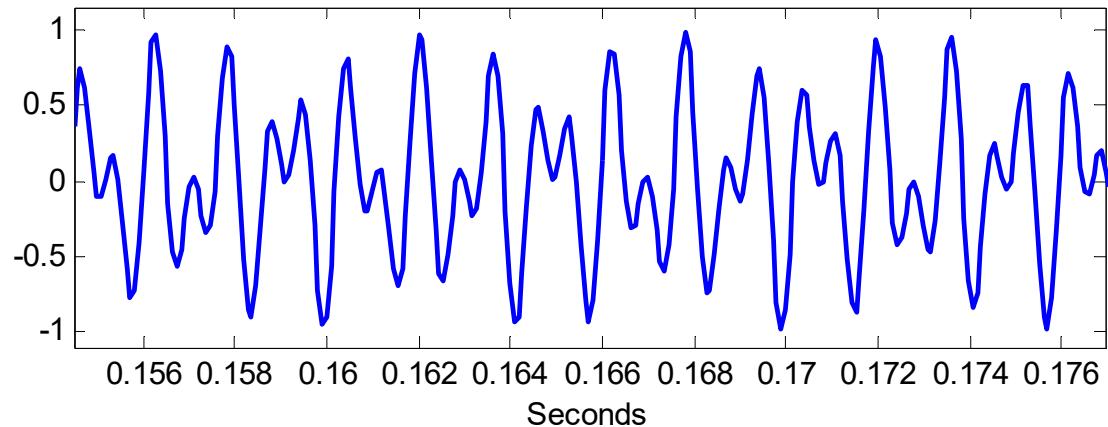
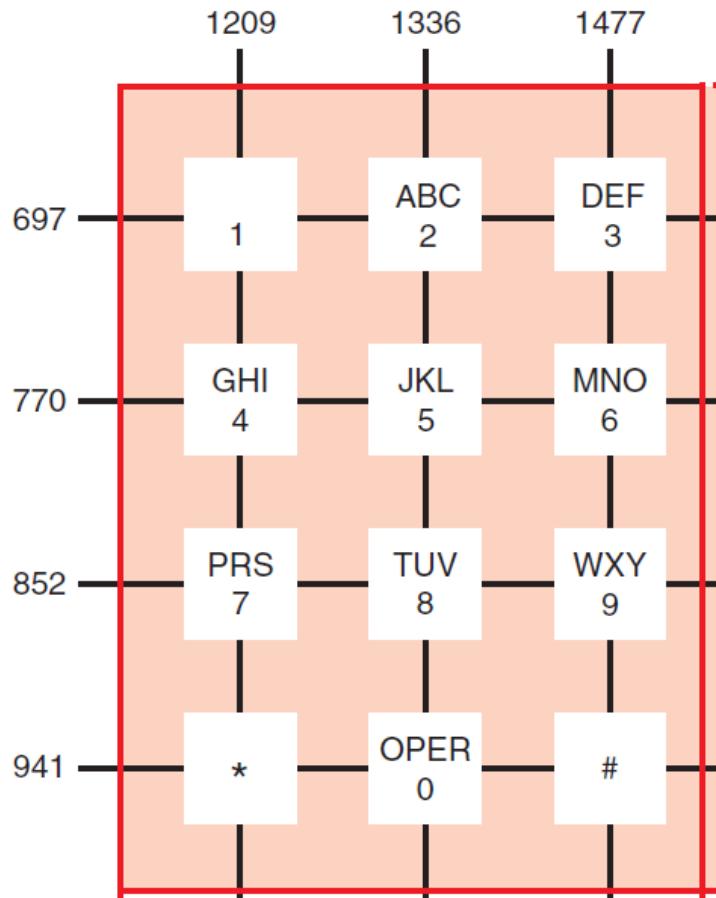
- Each number corresponds to a mix of two audio frequencies associated with each row and column of the corresponding pushbutton.



Most telephones use a standard keypad with 12 buttons or switches for the numbers 0 through 9 and the special symbols * and #.

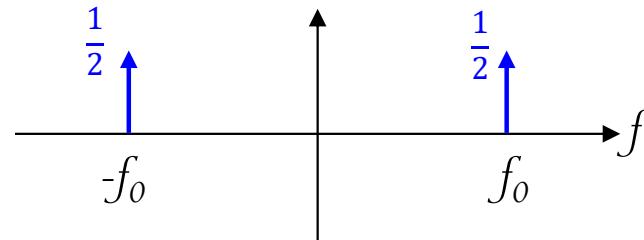
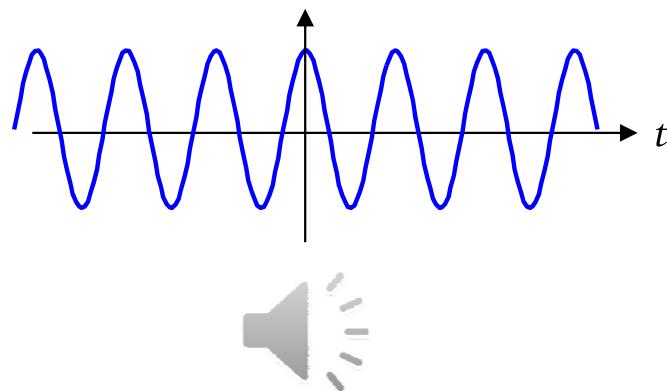
Four additional keys for special applications.

The “1” tone

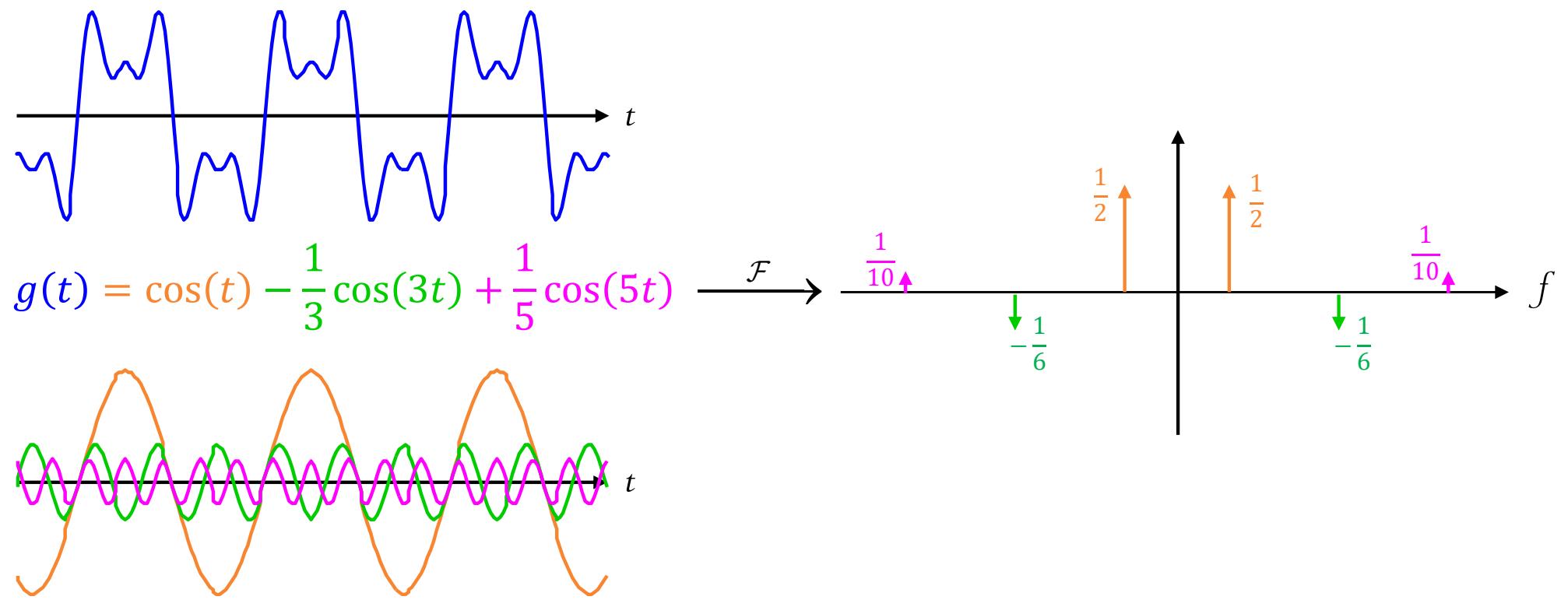


Fourier transform (\mathcal{F})

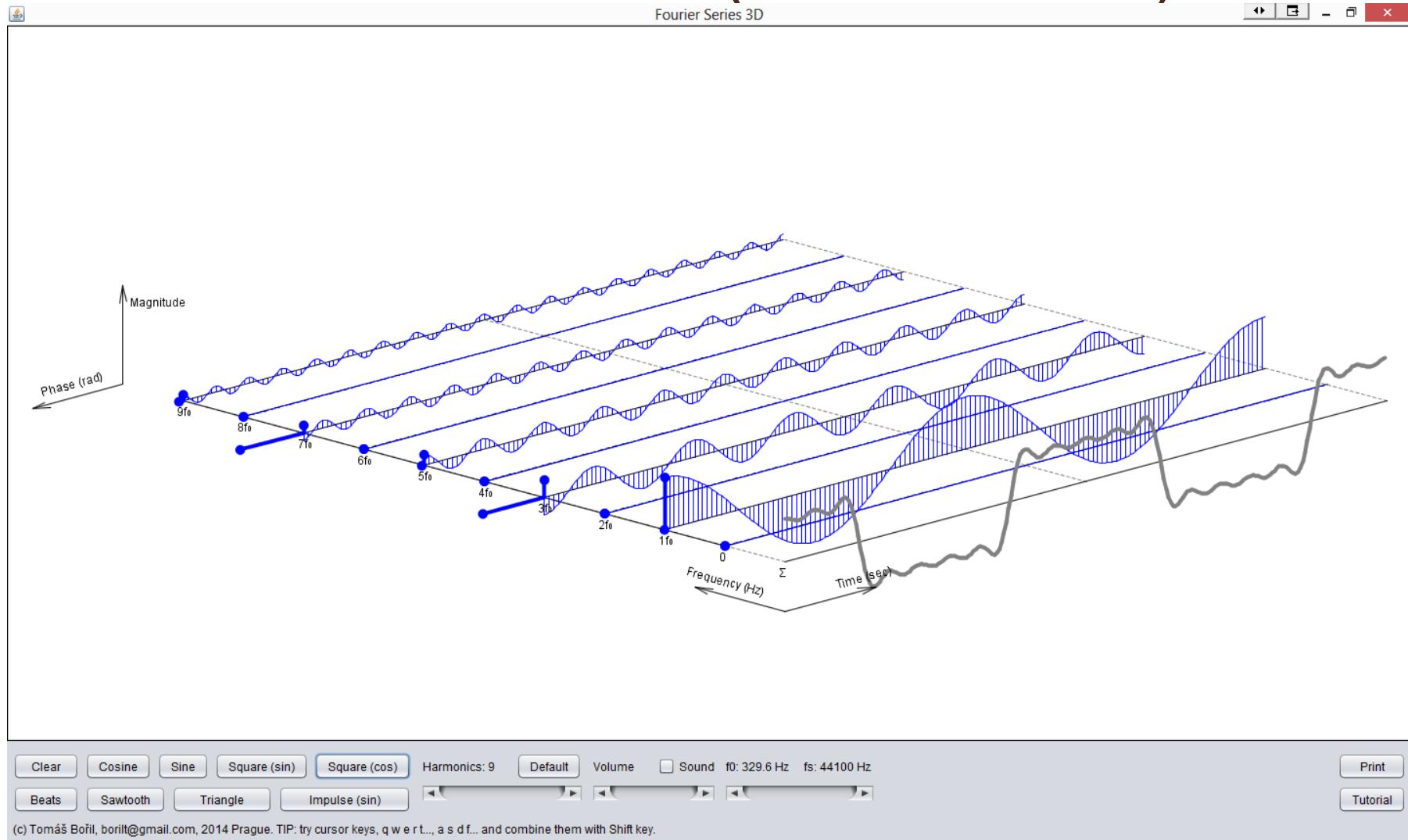
- The Fourier transform is a **frequency domain representation** of the original signal.
- The term Fourier transform refers to both the frequency domain representation and the corresponding mathematical operation (\mathcal{F}).



Fourier transform: Example



Fourier Series: Ex (interactive)



Euler's Formula

$$e^{j\theta} = \cos \theta + j \sin \theta$$

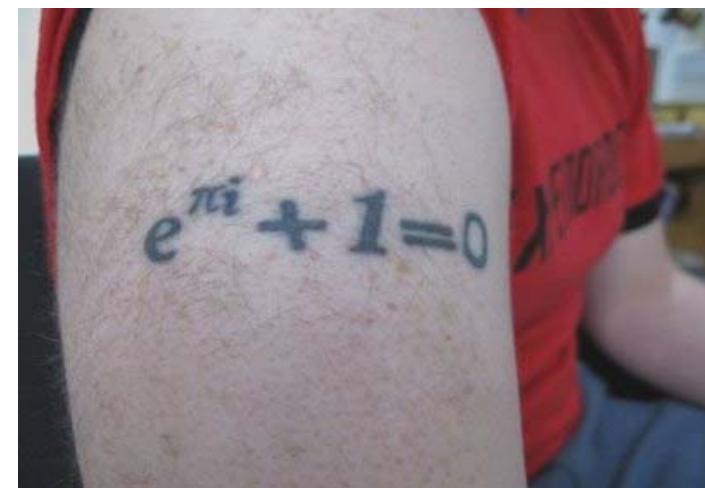
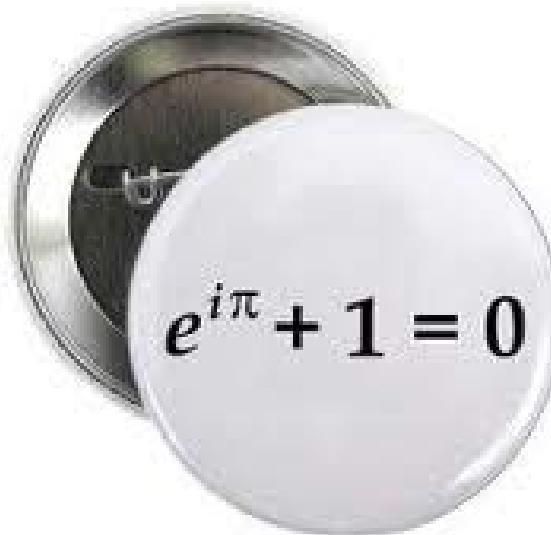


The Most Beautiful Equation

Euler's identity (Euler's equation)

Relate the three fundamental constants e, π and i.

Fact: When mathematicians describe equations as beautiful, they are not lying. Brain scans show that their minds respond to beautiful equations in the same way other people respond to great paintings or masterful music.



Euler's Formula

$$e^{j\theta} = \cos \theta + j \sin \theta$$

Complex
exponential

$$\cos(A) = \operatorname{Re}\{e^{jA}\} = \frac{1}{2}(e^{jA} + e^{-jA})$$

$$\sin(A) = \operatorname{Im}\{e^{jA}\} = \frac{1}{2j}(e^{jA} - e^{-jA})$$

$$\cos(-x) = \cos(x)$$

$$\cos\left(x - \frac{\pi}{2}\right) = \sin(x)$$

$$2\cos^2 x = 1 + \cos(2x)$$

$$2\sin^2 x = 1 - \cos(2x)$$

$$2\sin(x)\cos(x) = \sin(2x)$$

$$\frac{d}{dx} \sin x = \cos x$$

$$\cos(x)\cos(y) = \frac{1}{2}(\cos(x+y) + \cos(x-y))$$

(product-to-sum formula)

$$\text{Im}\{e^{j\theta}\} = \sin\theta$$

